

Design Principles of Programming Languages

## Practice

arith, fullsimple, fullref

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## Why learn type theories?

- Art vs. Knowledge
  - Art cannot be taught, while knowledge can
  - What people have invented
  - How to interpret them abstractly
  - How to reason their properties formally
- Why formal reasoning important
  - Poorly designed languages widely used
    - Java array flaw
    - JavaScript: google "JavaScript sucks"
    - PHP: you know it
  - Well designed language needs strictly reasoning
    - Devils in details



### Structure of arith



Main.ml drives the whole process.

Scan tokes (lexer.mll) Parse terms (parser.mly) Evaluate each terms (eval in core.ml)

Print the values (printtm in syntax.ml)

Syntax.ml defines the terms.



### Syntax.ml



type term =
 TmTrue of info
 ImFalse of info
 ImIf of info \* term \* term \* term
 ImZero of info
 ImSucc of info \* term
 ImPred of info \* term
 ImIsZero of info \* term

Info: a data type recording the position of the term in the source file



#### eval in core.ml



let rec eval t = try let t' = eval1 t in eval t' with NoRuleApplies → t

eval1: perform a single step reduction



### Commands



- Each line of the source file is parsed as a command
  - type command = | Eval of info \* term
  - New commands will be added later
- Main routine for each file

```
let process_file f =
    alreadyImported := f :: !alreadyImported;
```

```
let cmds = parseFile f in
```

```
letgc=
```

```
open_hvbox 0;
```

```
let results = process_command c in
```

```
print_flush();
```

```
results
```

```
in
```

```
List.iter g cmds
```



## Exercise arith.simple\_use



- Using arith to write the following equation
  - Return five if two is not zero, otherwise return nine
  - Hint: read the code in parser.mly



#### Exercise arith.size



- Make the evaluation computes the size of a term (3.3.2) instead of reducing the term
- Hint:
  - pr: string->unit prints a string to the screen
  - string\_of\_int : int->string converts an integer into a string
  - Remember to change both .ml and .mli files

- Some abbreviations
  - UCID = upper case identifier
  - LCID = lower case identifier
  - ty = type
  - tm = term
  - LCURLY = "{"
  - RCURLY = "}"
  - USCORE = "\_"



## Exercise arith.big-step



- Change the evaluation to use big-step semantics, and compare the results with small-step semantics on the following expressions
  - true;
  - if false then true else false;
  - if 0 then 1 else 2;
  - if true then (succ false) else 2;
  - 0;
  - succ (pred 0);
  - iszero (pred (succ (succ 0)));
- What does the comparison reveal?



## Big-step vs small-step



- Big-step is usually easier to understand
  - called "natural semantics" in some articles
- Big-step often leads to simpler proof
- Big-step cannot describe computations that do not produce a value
  - Non-terminating computation
  - "Stuck" computation



## fullsimple



- Implementing all extensions in Chapter 11
- Allow different types of command:
  - Evaluation: type-checking and reducing a term
  - Bindings
    - Variable binding: a:Int;
    - Type variable binding: T;
    - Term abbreviation binding: t = succ 0;
    - Type abbreviation binding: T = Nat -> Nat;
- Types can be used without declaration (uninterpreted types)
  - x:X

(lambda a:X. a) x



## Review: nameless representation



- What is the nameless representation of the following term?
  - $\lambda x. x (\lambda y. x y)$

•  $\lambda$ . 0 ( $\lambda$ . 1 0)



## fullsimple, terms



```
type term =
  TmVar of info * int * int
   TmAbs of info * string * ty * term
   TmApp of info * term * term
   I..
```

- Using nameless representation of terms
- The second int for TmVar is used for debugging
  - = the number of items in the context
- The "string" in TmAbs is used for printing



## Example: printing terms



```
and printtm ATerm outer ctx t = match t with
 | TmVar(fi,x,n) ->
   if ctxlength ctx = n then
    pr (index2name fi ctx x)
   else
    pr ("[bad index: " ^ ...
TmAbs(fi,x,tyT1,t2) ->
   (let (ctx',x') = (pickfreshname ctx x) in
     obox(); pr "lambda ";
     pr x'; pr ":"; printty Type false ctx tyT1; pr "."; ...
     printtm Term outer ctx' t2; ...
```



#### Review: context

- What contexts are used in our course?
  - Mapping names to integers in nameless representation
  - $\Sigma$ : mapping variables to types
- Can be combined into one
- New contexts in the implementation
  - Type variable binding: marking type variables
  - Term abbreviation binding: Mapping variables to terms (and their types)
  - Type abbreviation binding: Mapping type variables to terms
- All can be combined into one

Only used in printing as a placeholder



type binding =
 NameBind
 TyVarBind
 VarBind of ty
 TmAbbBind of term \* (ty option)
 TyAbbBind of ty
 type context = (string \* binding) list

Queried by index



## Auxiliary functions for nameless representation

- name2index
  - info->context
     ->string->int
  - return the index of a name
- index2name
  - info->context
     ->int->string
  - inverse of the above
- pickfreshname
  - context->string
     ->(context, string)
  - generate a fresh name using the second parameter as hint

type binding =
 NameBind
 TyVarBind
 VarBind of ty
 TmAbbBind of term \* (ty option)
 TyAbbBind of ty





## Exercise fullsimple.nameless



 Construct a term t that is evaluated a term t' in fullsimple, where t' is different from t via only alpha-renaming (i.e., no beta-reduction)



## Exercise for fullsimple.rec\_fix



- Define plus using fix and test the following expressions
  - plus 10 105;
  - plus 0 1;
  - plus 0 0;
  - plus 2 0;



## Exercise fullref.rec\_no\_fix



• Write plus without using fix or letrec in fullref



#### Exercise fullsimple.natlist



• Try the following term in fullsimple and explain why it cannot be typed

NatList = <nil:Unit, cons:{Nat,NatList}>;

nil = <nil=unit> as NatList;

cons = lambda n:Nat. lambda l:NatList. <cons={n,l}> as NatList;



## Exercise fullsimple.match



- Add pattern matching for tuples, and test on the following expressions
  - let {x, y, z} = {true, 1, {2}} in z;
  - let {x, y, z} = {true, 1, {2}} in (lambda x:Nat. x) y;
  - let {x, y, z} = let x = 1 in {true, x, {2}} in z;
  - lambda x:Nat. let {x, y} = {true, 1} in x;
  - let x = 0 in let {y, z} = {1, 2} in x;
  - let {y, z} = {1, 2} in let y = 3 in y;
- Part of the code is already provided to you in the following two pages



# Partial code for fullsimple.match



- Adding the following line to "type term =" in syntax.ml
  - | TmPLet of info \* string list \* term \* term
- Adding the following lines after line 235 in parser.mly
  - | LET Pattern EQ Term IN Term
  - { fun ctx -> TmPLet(\$1, \$2, \$4 ctx, \$6 (List.fold\_left (fun x y -> addname x y) ctx \$2)) }
  - Pattern :
  - LCURLY MetaVars RCURLY
  - {\$2}
  - | LCURLY RCURLY
  - { [] }

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- Add the following line to tminfo in syntax.ml
  - | TmPLet(fi,\_,\_,\_) -> fi



# Partial code for fullsimple.match



- Adding the following lines to "printtm\_Term" in syntax.ml
  - | TmPLet(fi, xs, t1, t2) ->
  - obox0();
  - pr "let {";
  - let rec print xs =
  - match xs with
  - x::x'::rest -> pr x; pr ","; print (x'::rest);
  - | x::[] -> pr x;
  - | [] -> pr ""; in
  - print xs;
  - pr "} = ";
  - printtm\_Term false ctx t1;
  - print\_space(); pr "in"; print\_space();
  - let ctx' = List.fold\_left (fun ctx x -> addname ctx x) ctx xs in
  - printtm\_Term false ctx' t2;
  - cbox()



#### Homework



- Finish fullsimple.match
- Submit your code as a compressed file with one of the above names
- Your submission should contain file test.f which contains exactly the expressions to be tested
- TA will perform the following two commands to verify your submission:
  - make
  - ./f test.f

