



Design Principles of Programming Languages

Practice

arith, fullsimple, fullref

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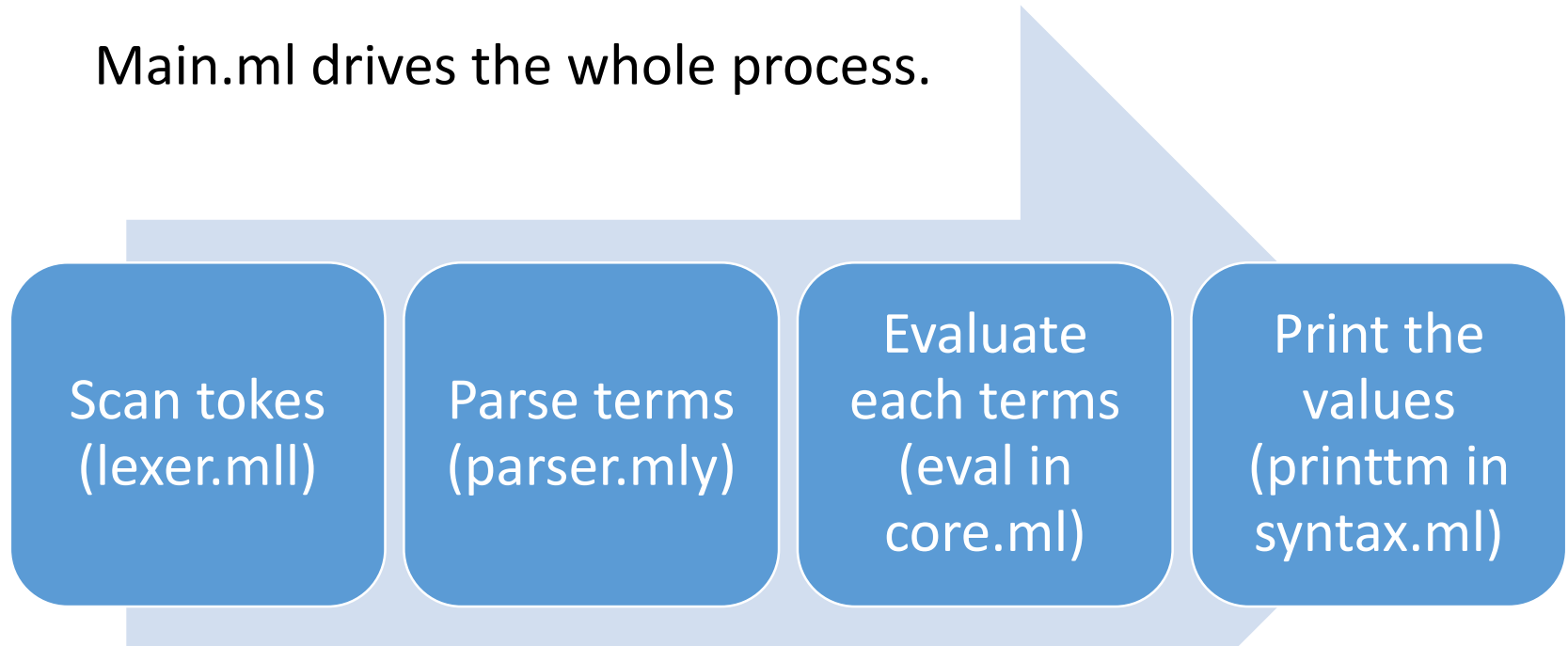
Why learn type theories?

- Art vs. Knowledge
 - Art cannot be taught, while knowledge can
 - What people have invented
 - How to interpret them abstractly
 - How to reason their properties formally
- Why formal reasoning important
 - Poorly designed languages widely used
 - Java array flaw
 - JavaScript: google “JavaScript sucks”
 - PHP: you know it
 - Well designed language needs strictly reasoning
 - Devils in details



Structure of arith

Main.ml drives the whole process.



Syntax.ml defines the terms.



Syntax.ml

```
type term =  
  TmTrue of info  
| TmFalse of info  
| TmIf of info * term * term * term  
| TmZero of info  
| TmSucc of info * term  
| TmPred of info * term  
| TmIsZero of info * term
```

Info: a data type recording the position of the term in the source file



eval in core.ml

```
let rec eval t =  
  try let t' = eval1 t  
    in eval t'  
  with NoRuleApplies → t
```

eval1: perform a single step reduction



Commands

- Each line of the source file is parsed as a command
 - type command = | Eval of info * term
 - New commands will be added later

- Main routine for each file

```
let process_file f =  
  alreadyImported := f :: !alreadyImported;  
  let cmds = parseFile f in  
  let g c =  
    open_hvbox 0;  
    let results = process_command c in  
    print_flush();  
    results  
  in  
  List.iter g cmds
```



Exercise arith.simple_use

- Using arith to write the following equation
 - Return five if two is not zero, otherwise return nine
 - Hint: read the code in parser.mly



Exercise arith.size

- Make the evaluation computes the size of a term (3.3.2) instead of reducing the term
- Hint:
 - `pr: string->unit` prints a string to the screen
 - `string_of_int : int->string` converts an integer into a string
 - Remember to change both `.ml` and `.mli` files
- Some abbreviations
 - UCID = upper case identifier
 - LCID = lower case identifier
 - `ty` = type
 - `tm` = term
 - LCURLY = “{”
 - RCURLY = “}”
 - USCORE = “_”



Exercise arith.big-step

- Change the evaluation to use big-step semantics, and compare the results with small-step semantics on the following expressions
 - true;
 - if false then true else false;
 - if 0 then 1 else 2;
 - if true then (succ false) else 2;
 - 0;
 - succ (pred 0);
 - iszero (pred (succ (succ 0)));
- What does the comparison reveal?



Big-step vs small-step

- Big-step is usually easier to understand
 - called “natural semantics” in some articles
- Big-step often leads to simpler proof
- Big-step cannot describe computations that do not produce a value
 - Non-terminating computation
 - “Stuck” computation



fullsimple

- Implementing all extensions in Chapter 11
- Allow different types of command:
 - Evaluation: type-checking and reducing a term
 - Bindings
 - Variable binding: $a:\text{Int}$;
 - Type variable binding: T ;
 - Term abbreviation binding: $t = \text{succ } 0$;
 - Type abbreviation binding: $T = \text{Nat} \rightarrow \text{Nat}$;
- Types can be used without declaration (uninterpreted types)
 - $x:X$
 - $(\text{lambda } a:X. a) x$



Review: nameless representation

- What is the nameless representation of the following term?
 - $\lambda x. x (\lambda y. x y)$

- $\lambda. 0 (\lambda. 1 0)$



fullsimple, terms

type term =

TmVar of info * int * int

| TmAbs of info * string * ty * term

| TmApp of info * term * term

| ..

- Using nameless representation of terms
- The second int for TmVar is used for debugging
 - = the number of items in the context
- The “string” in TmAbs is used for printing



Example: printing terms

and printtm_ATerm outer ctx t = match t with

| TmVar(fi,x,n) ->

if ctxlength ctx = n then

pr (index2name fi ctx x)

else

pr ("[bad index: " ^ ...

| TmAbs(fi,x,tyT1,t2) ->

(let (ctx',x') = (pickfreshname ctx x) in

obox(); pr "lambda ";

pr x'; pr ":"; printty_Type false ctx tyT1; pr "."; ...

printtm_Term outer ctx' t2; ...



Review: context

Only used in printing as a placeholder

- What contexts are used in our course?
 - Mapping names to integers in nameless representation
 - Σ : mapping variables to types
- Can be combined into one
- New contexts in the implementation
 - Type variable binding: marking type variables
 - Term abbreviation binding: Mapping variables to terms (and their types)
 - Type abbreviation binding: Mapping type variables to terms
- All can be combined into one

```
type binding =  
  NameBind  
  | TyVarBind  
  | VarBind of ty  
  | TmAbbBind of term * (ty option)  
  | TyAbbBind of ty  
  
type context = (string * binding) list
```

Queried by index



Auxiliary functions for nameless representation

- name2index
 - info->context
->string->int
 - return the index of a name
- index2name
 - info->context
->int->string
 - inverse of the above
- pickfreshname
 - context->string
->(context, string)
 - generate a fresh name using the second parameter as hint

```
type binding =  
  NameBind  
  | TyVarBind  
  | VarBind of ty  
  | TmAbbBind of term * (ty option)  
  | TyAbbBind of ty  
  
type context = (string * binding) list
```




Exercise fullsimple.nameless

- Construct a term t that is evaluated a term t' in fullsimple, where t' is different from t via only alpha-renaming (i.e., no beta-reduction)



Exercise fullsimple.rec_fix

- Define plus using fix and test the following expressions
 - plus 10 105;
 - plus 0 1;
 - plus 0 0;
 - plus 2 0;



Exercise fullsimple.natlist

- Try the following term in fullsimple and explain why it cannot be typed

```
NatList = <nil:Unit, cons:{Nat,NatList}>;
```

```
nil = <nil=unit> as NatList;
```

```
cons = lambda n:Nat. lambda l:NatList. <cons={n,l}> as  
NatList;
```



Exercise fullsimple.match

- Add pattern matching for tuples, and test on the following expressions
 - $\text{let } \{x, y, z\} = \{\text{true}, 1, \{2\}\} \text{ in } z;$
 - $\text{let } \{x, y, z\} = \{\text{true}, 1, \{2\}\} \text{ in } (\text{lambda } x:\text{Nat. } x) y;$
 - $\text{let } \{x, y, z\} = \text{let } x = 1 \text{ in } \{\text{true}, x, \{2\}\} \text{ in } z;$
 - $\text{lambda } x:\text{Nat. } \text{let } \{x, y\} = \{\text{true}, 1\} \text{ in } x;$
 - $\text{let } x = 0 \text{ in } \text{let } \{y, z\} = \{1, 2\} \text{ in } x;$
 - $\text{let } \{y, z\} = \{1, 2\} \text{ in } \text{let } y = 3 \text{ in } y;$
- Part of the code is already provided to you in the following two pages



Partial code for fullsimple.match

- Adding the following line to “type term =” in syntax.ml
 - | TmPLet of info * string list * term * term
- Adding the following lines after line 235 in parser.mly
 - | LET Pattern EQ Term IN Term
 - { fun ctx -> TmPLet(\$1, \$2, \$4 ctx, \$6 (List.fold_left (fun x y -> addname x y) ctx \$2)) }
 - Pattern :
 - LCURLY MetaVars RCURLY
 - { \$2 }
 - | LCURLY RCURLY
 - { [] }
- Add the following line to tminfo in syntax.ml
 - | TmPLet(fi,_,_,_) -> fi



Partial code for fullsimple.match

- Adding the following lines to “printtm_Term” in syntax.ml
 - | TmPLet(fi, xs, t1, t2) ->
 - obox0();
 - pr "let {";
 - let rec print xs =
 - match xs with
 - x::x'::rest -> pr x; pr ","; print (x'::rest);
 - | x::[] -> pr x;
 - | [] -> pr "";
 - in
 - print xs;
 - pr "} = ";
 - printtm_Term false ctx t1;
 - print_space(); pr "in"; print_space();
 - let ctx' = List.fold_left (fun ctx x -> addname ctx x) ctx xs in
 - printtm_Term false ctx' t2;
 - cbox()



Homework

- Finish `fullsimple.match`
- Submit your code as a compressed file with one of the above names
- Your submission should contain file `test.f` which contains exactly the expressions to be tested
- TA will perform the following two commands to verify your submission:
 - `make`
 - `./f test.f`