#### Design Principles of Programming Languages

## Practice

arith, fullsimple

Zhenjiang Hu, Haiyan Zhao, <u>Yingfei Xiong</u>
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## Why learn type theories?



- Art vs. Knowledge
  - Art cannot be taught, while knowledge can
  - What people have invented
  - How to interpret them abstractly
  - How to reason their properties formally
- Why formal reasoning important
  - Poorly designed languages widely used
    - Java array flaw
    - JavaScript: google "JavaScript sucks"
    - PHP: you know it
  - Well designed language needs strictly reasoning
    - Devils in details



#### Structure of arith



Main.ml drives the whole process.

Scan tokes (lexer.mll)

Parse terms (parser.mly)

Evaluate each terms (eval in core.ml)

Print the values (printtm in syntax.ml)

Syntax.ml defines the terms.



## Syntax.ml



```
type term =
    TmTrue of info
    | TmFalse of info
    | TmIf of info * term * term * term
    | TmZero of info
    | TmSucc of info * term
    | TmPred of info * term
    | TmIsZero of info * term
```

Info: a data type recording the position of the term in the source file



#### eval in core.ml



```
let rec eval t =
  try let t' = eval1 t
    in eval t'
  with NoRuleApplies → t
```

eval1: perform a single step reduction



#### Commands



- Each line of the source file is parsed as a command
  - type command = | Eval of info \* term
  - New commands will be added later
- Main routine for each file

```
let process_file f =
  alreadyImported := f :: !alreadyImported;
let cmds = parseFile f in
  let g c =
    open_hvbox 0;
  let results = process_command c in
    print_flush();
  results
  in
    List.iter g cmds
```



#### Exercise arith.simple\_use



- Using arith to write the following equation
  - Return five if two is zero, otherwise return nine
  - Hint: read the code in parser.mly



#### Exercise arith.size



- Make the evaluation computes the size of a term (3.3.2) instead of reducing the term
- Hint:
  - pr: string->unit prints a string to the screen
  - string\_of\_int : int->string converts an integer into a string
  - Remember to change both .ml and .mli files

- Some abbreviations
  - UCID = upper case identifier
  - LCID = lower case identifier
  - ty = type
  - tm = term
  - LCURLY = "{"
  - RCURLY = "}"
  - USCORE = "\_"



#### Exercise arith.big-step



- Change the evaluation to use big-step semantics, and compare the results with small-step semantics on the following expressions
  - true;
  - if false then true else false;
  - if 0 then 1 else 2;
  - if true then (succ false) else 2;
  - 0;
  - succ (pred 0);
  - iszero (pred (succ (succ 0)));
- What does the comparison reveal?



#### Big-step vs small-step



- Big-step is usually easier to understand
  - called "natural semantics" in some articles
- Big-step often leads to simpler proof
- Big-step cannot describe computations that do not produce a value
  - Non-terminating computation
  - "Stuck" computation



## fullsimple



- Implementing all extensions in Chapter 11
- Allow different types of command:
  - Evaluation: type-checking and reducing a term
  - Bindings
    - Variable binding: a:Int;
    - Type variable binding: T;
    - Term abbreviation binding: t = succ 0;
    - Type abbreviation binding: T = Nat -> Nat;
- Types can be used without declaration (uninterpreted types)

```
x:X (lambda a:X. a) x
```



# Review: nameless representation



- What is the nameless representation of the following term?
  - $\lambda x. x (\lambda y. x y)$

•  $\lambda$ . 0 ( $\lambda$ . 1 0)



### fullsimple, terms



```
type term =
   TmVar of info * int * int
   | TmAbs of info * string * ty * term
   | TmApp of info * term * term
   | ..
```

- Using nameless representation of terms
- The second int for TmVar is used for debugging
  - = the number of items in the context
- The "string" in TmAbs is used for printing



## Example: printing terms



```
and printtm ATerm outer ctx t = match t with
 | TmVar(fi,x,n) ->
   if ctxlength ctx = n then
    pr (index2name fi ctx x)
   else
    pr ("[bad index: " ^ ...
| TmAbs(fi,x,tyT1,t2) ->
   (let (ctx',x') = (pickfreshname ctx x) in
     obox(); pr "lambda ";
     pr x'; pr ":"; printty Type false ctx tyT1; pr "."; ...
     printtm Term outer ctx' t2; ...
```



#### Review: context

Only used in printing as a placeholder



- What contexts are used in our course?
  - Mapping names to integers in nameless representation
  - Σ: mapping variables to types
- Can be combined into one
- New contexts in the implementation
  - Type variable binding: marking type variables
  - Term abbreviation binding: Mapping variables to terms (and their types)
  - Type abbreviation binding: Mapping type variables to terms
- All can be combined into one

type/binding =
 NameBind
 | TyVarBind
 | VarBind of ty
 | TmAbbBind of term \* (ty option)
 | TyAbbBind of ty

type context = (string \* binding) list

Queried by index



## Auxiliary functions for nameless representation



- name2index
  - info->context->string->int
  - return the index of a name
- index2name
  - info->context->int->string
  - inverse of the above
- pickfreshname
  - context->string->(context, string)
  - generate a fresh name using the second parameter as hint

```
type binding =

NameBind
| TyVarBind
| VarBind of ty
| TmAbbBind of term * (ty option)
| TyAbbBind of ty
```

type context = (string \* binding) list



### Exercise fullsimple.nameless



 Construct a term t that is evaluated a term t' in fullsimple, where t' is different from t via only alpha-renaming (i.e., no beta-reduction)



#### Exercise fullsimple.natlist



 Try the following term in fullsimple and explain why it cannot be typed

```
NatList = <nil:Unit, cons:{Nat,NatList}>;
nil = <nil=unit> as NatList;
cons = lambda n:Nat. lambda l:NatList. <cons={n,l}> as NatList;
```



#### Exercise fullsimple.match



- Add pattern matching for tuples, and test on the following expressions
  - let {x, y, z} = {true, 1, {2}} in z;
  - let {x, y, z} = {true, 1, {2}} in (lambda x:Nat. x) y;
  - let {x, y, z} = let x = 1 in {true, x, {2}} in z;
  - lambda x:Nat. let {x, y} = {true, 1} in x;
  - let x = 0 in let {y, z} = {1, 2} in x;
  - let  $\{y, z\} = \{1, 2\}$  in let y = 3 in y;
- Part of the code is already provided to you in the following two pages



# Partial code for fullsimple.match



- Adding the following line to "type term =" in syntax.ml
  - | TmPLet of info \* string list \* term \* term
- Adding the following lines after line 235 in parser.mly
  - LET Pattern EQ Term IN Term
  - { fun ctx -> TmPLet(\$1, \$2, \$4 ctx, \$6 (List.fold\_left (fun x y -> addname x y) ctx \$2)) }
  - Pattern:
  - LCURLY MetaVars RCURLY
  - {\$2}
  - LCURLY RCURLY
  - {[]}
- Add the following line to tminfo in syntax.ml
  - | TmPLet(fi,\_\_,\_\_) -> fi



## Partial code for fullsimple.match



- Adding the following lines to "printtm\_Term" in syntax.ml
  - | TmPLet(fi, xs, t1, t2) -> obox0();pr "let {"; let rec print xs = match xs with x::x'::rest -> pr x; pr ","; print (x'::rest); | x::[] -> pr x; | [] -> pr ""; in print xs; pr "} = "; printtm Term false ctx t1; print\_space(); pr "in"; print\_space(); let ctx' = List.fold\_left (fun ctx x -> addname ctx x) ctx xs in printtm\_Term false ctx' t2; cbox()



## Exercise fullsimple.let



Do exercise 11.5.1 letexercise

• Try not to seek the answer. Figure it out independently.



#### Homework



- Finish fullsimple.match
- Submit your code as a compressed file
- Your submission should contain file test.f which contains exactly the expressions to be tested
- TA will perform the following two commands to verify your submission:
  - make
  - ./f test.f

