



软件分析

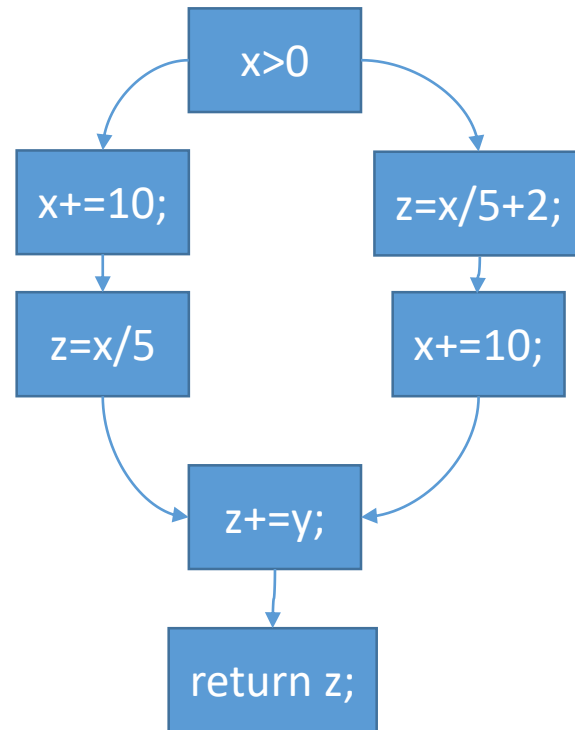
# 符号执行

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2016



# 符号执行

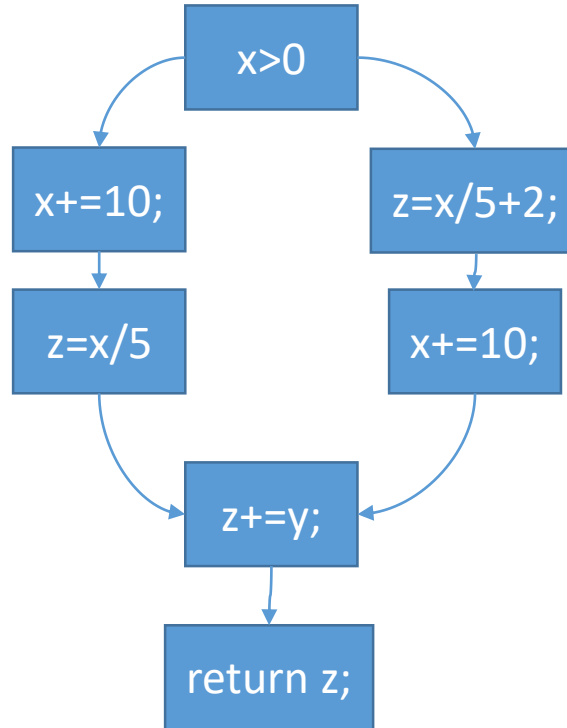
- `int main(x,y) {`
- `if (x>0) {`
- `x+=10;`
- `z=x/5;`
- `}`
- `else {`
- `z=x/5+2;`
- `x+=10;`
- `}`
- `z+=y;`
- `return z;`
- `}`





# 符号执行

- `int main(x,y) {`
- `if (x>0) {`
- `x+=10;`
- `z=x/5;`
- `}`
- `else {`
- `z=x/5+2;`
- `x+=10;`
- `}`
- `z+=y;`
- `return z;`
- `}`

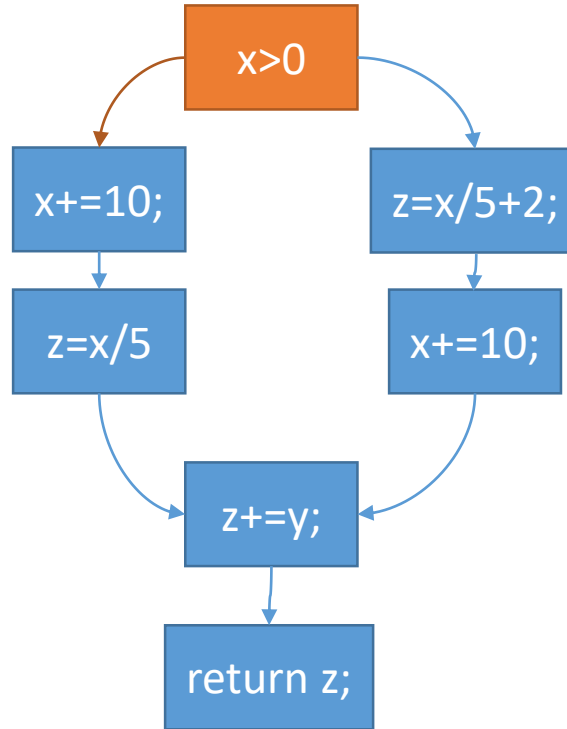


x=a  
y=b  
z=?



# 符号执行

- `int main(x,y) {`
- `if (x>0) {`
- `x+=10;`
- `z=x/5;`
- `}`
- `else {`
- `z=x/5+2;`
- `x+=10;`
- `}`
- `z+=y;`
- `return z;`
- `}`

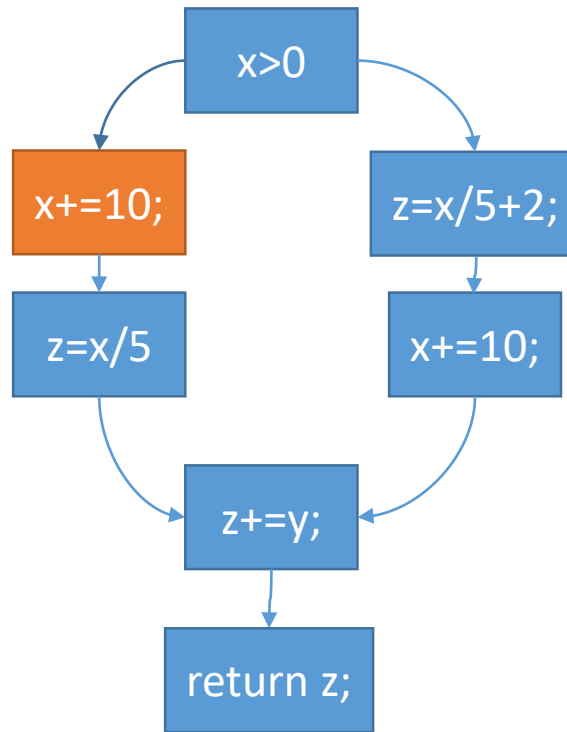


x=a  
y=b  
z=?  
a>0



# 符号执行

- `int main(x,y) {`
- `if (x>0) {`
- `x+=10;`
- `z=x/5;`
- `}`
- `else {`
- `z=x/5+2;`
- `x+=10;`
- `}`
- `z+=y;`
- `return z;`
- `}`

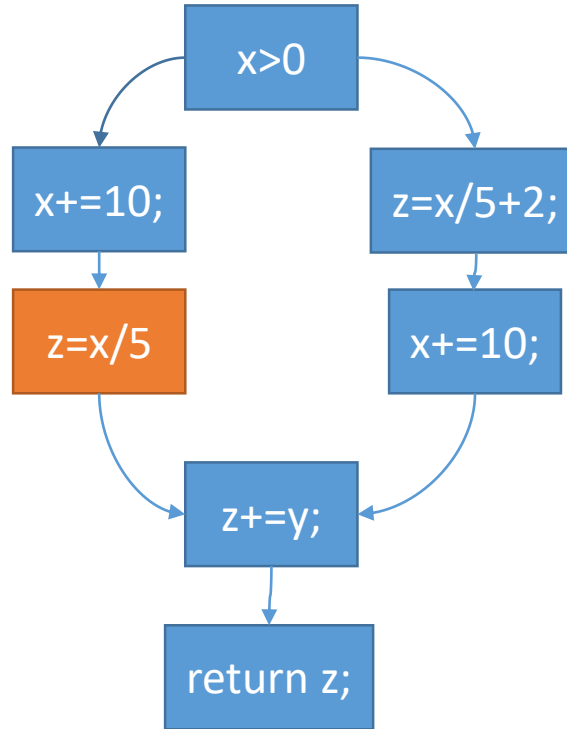


x=a+10  
y=b  
z=?  
a>0



# 符号执行

- `int main(x,y) {`
- `if (x>0) {`
- `x+=10;`
- `z=x/5;`
- `}`
- `else {`
- `z=x/5+2;`
- `x+=10;`
- `}`
- `z+=y;`
- `return z;`
- `}`

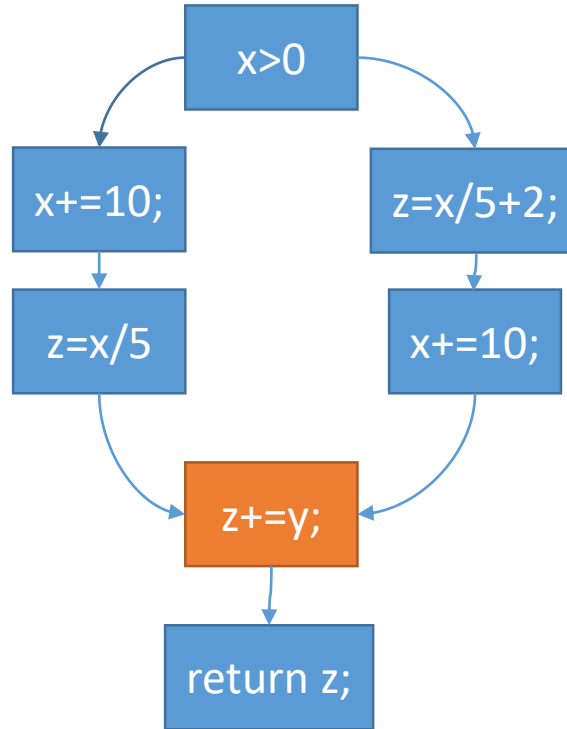


`x=a+10`  
`y=b`  
`z=(a+10)/5`  
`a>0`



# 符号执行

- `int main(x,y) {`
- `if (x>0) {`
- `x+=10;`
- `z=x/5;`
- `}`
- `else {`
- `z=x/5+2;`
- `x+=10;`
- `}`
- `z+=y;`
- `return z;`
- `}`

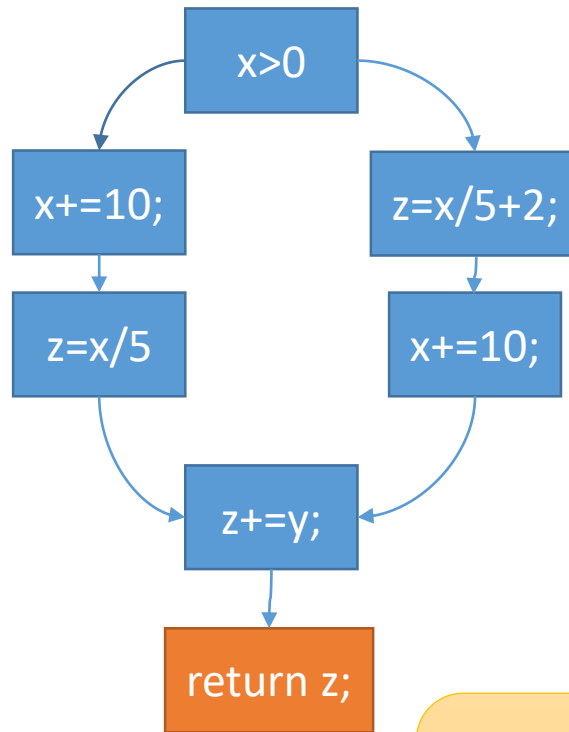


`x=a+10`  
`y=b`  
`z=(a+10)/5+b`  
`a>0`



# 符号执行

- `int main(x,y) {`
- `if (x>0) {`
- `x+=10;`
- `z=x/5;`
- `}`
- `else {`
- `z=x/5+2;`
- `x+=10;`
- `}`
- `z+=y;`
- `return z;`
- `}`



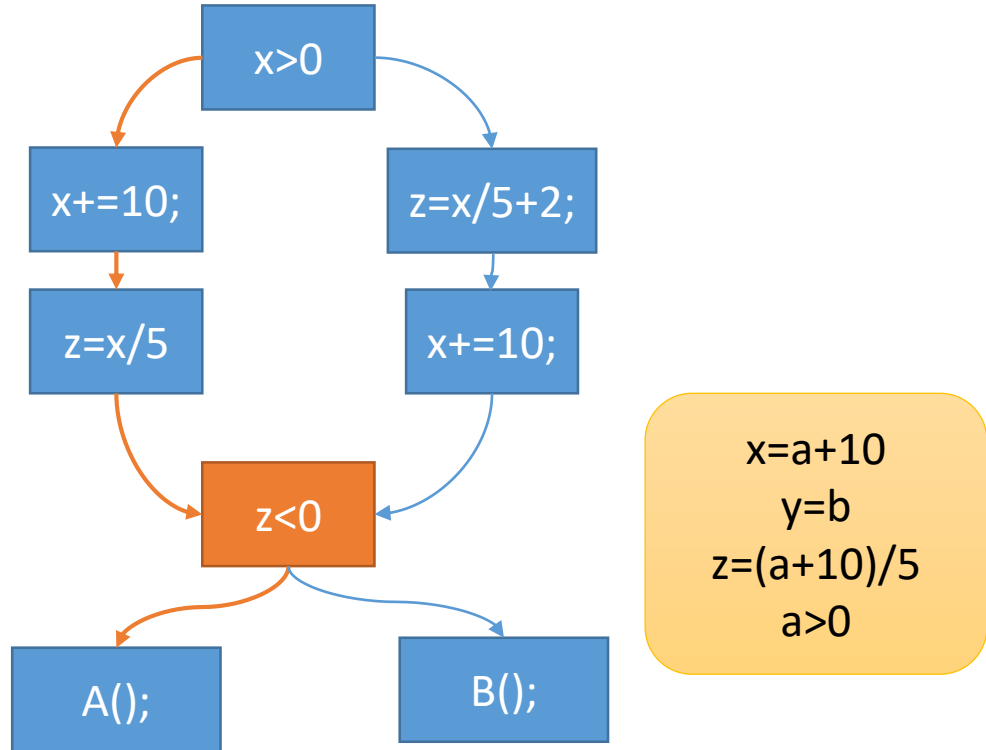
$x=a+10$   
 $y=b$   
 $z=(a+10)/5+b$   
 $a>0$

返回值为 $(a+10)/5+b$   
且 $a>0$





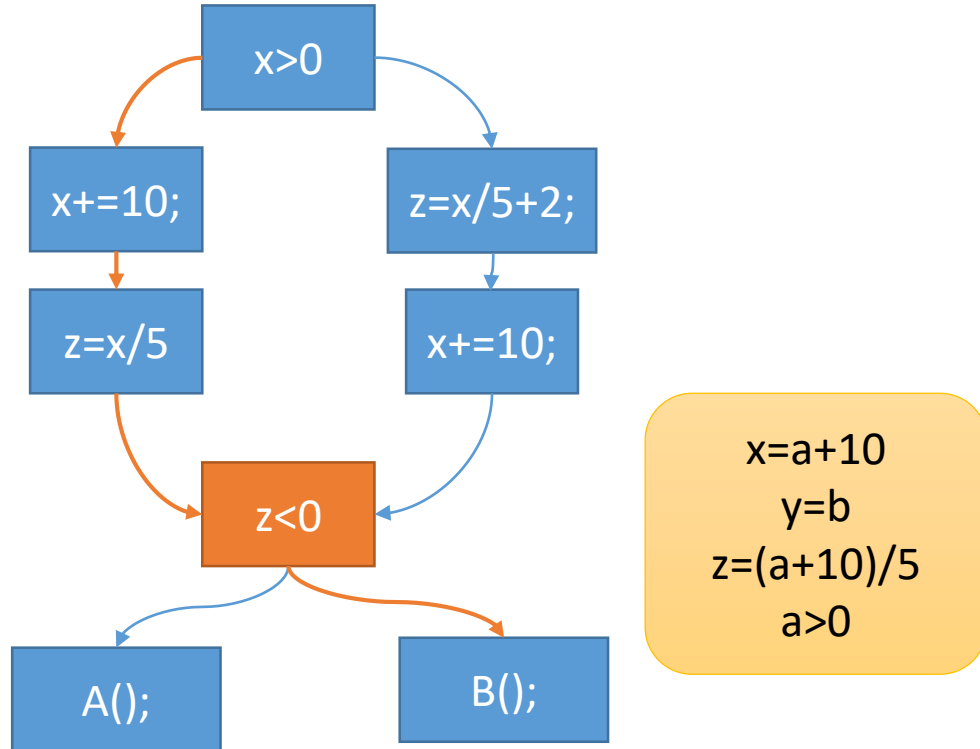
# 路径可行性



$a > 0 \wedge (a + 10) / 5 < 0$  不可满足



# 路径可行性



$x=a+10$   
 $y=b$   
 $z=(a+10)/5$   
 $a>0$

$a>0 \wedge (a+10)/5 < 0$  不可满足



# 符号执行

- 程序的规约通常表示为前条件和后条件
  - 前条件:  $a > 0, b > 0$
  - 后条件:  $\text{return} > 0$
- 形成命题:
  - $a > 0 \wedge b > 0 \Rightarrow (a+10)/5 + b > 0$
  - 命题成立=逆命题不可满足
  - 用SMT Solver可求解
- 规约被违反=任意路径对应的命题不成立
- 规范被满足=所有路径对应的命题都成立
  - 通常做不到
  - 对于循环, 遍历有限次



# 符号执行的应用

## 除0错误

```
if (i != 0)
    x = 3 / i;
else
    ERROR;
```

## 缓冲区溢出错误

```
if (0 <= i && i < a.length)
    a[i] = 4;
else
    ERROR;
```



# 约束求解失败的情况

- 形成了复杂条件
  - $x^5 + 3x^3 == y$
  - `p->next->value == x`
- 调用了系统调用
  - `if (file.read()==x)`
- 动态符号执行
  - 混合程序的真实执行和符号执行
  - 在约束求解无法进行的时候，用真实值代替符号值
    - 如果真实值 $x=10$ ，则 $x^5 + 3x^3 == y$ 变为 $103000==y$ ，可满足



# 动态符号执行

- 动态符号执行主要用于生成测试输入
- 代表性工作：
  - Concolic Testing, Koushik Sen
    - 主要工具: CUTE
  - Execution-Generated Testing, Cristian Cadar
    - 主要工具: KLEE

# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;  
}
```

```
void testme (int x, int y) {
```

```
    ← z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete  
Execution

concrete  
state

x = 22, y = 7

Symbolic  
Execution

symbolic  
state

x = x<sub>0</sub>, y = y<sub>0</sub>

path  
condition

# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;  
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete  
Execution

Symbolic  
Execution

concrete  
state

symbolic  
state

path  
condition

$x = 22, y = 7, z = 14$

$x = x_0, y = y_0, z = 2 * y_0$



# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;  
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete  
Execution

Symbolic  
Execution

concrete  
state

symbolic  
state

path  
condition

$x = 22, y = 7, z = 14$

$x = x_0, y = y_0, z = 2*y_0$

$2*y_0 \neq x_0$

# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete Execution

Symbolic Execution

concrete state

symbolic state

path condition

Solve:  $2 * y_0 == x_0$   
 Solution:  $x_0 = 2, y_0 = 1$

$2 * y_0 != x_0$

$x = 22, y = 7, z = 14$

$x = x_0, y = y_0, z = 2 * y_0$

# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;  
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete  
Execution

Symbolic  
Execution

concrete  
state

symbolic  
state

path  
condition

$x = 2, y = 1$

$x = x_0, y = y_0$

# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete Execution

Symbolic Execution

concrete state

symbolic state

path condition

$x = 2, y = 1, z = 2$

$x = x_0, y = y_0, z = 2 * y_0$



# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        ← if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete Execution

Symbolic Execution

concrete state

symbolic state

path condition

$x = 2, y = 1, z = 2$

$x = x_0, y = y_0, z = 2 * y_0$

$2 * y_0 == x_0$

# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete  
Execution

Symbolic  
Execution

concrete  
state

symbolic  
state

path  
condition

$2 * y_0 == x_0$

$x_0 > y_0 + 10$

$x = 2, y = 1,$

$z = 2$

$x = x_0, y = y_0, z = 2 * y_0$



# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete Execution

Symbolic Execution

concrete state

symbolic state

path condition

Solve:  $(2 * y_0 == x_0) \wedge (x_0 > y_0 + 10)$   
 Solution:  $x_0 = 30, y_0 = 15$

$2 * y_0 == x_0$

$x_0 > y_0 + 10$

$x = 2, y = 1, z = 2$

$x = x_0, y = y_0, z = 2 * y_0$



# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;  
}
```

```
void testme (int x, int y) {
```

```
    ← z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete  
Execution

concrete  
state

x = 30, y = 15

Symbolic  
Execution

symbolic  
state

x = x<sub>0</sub>, y = y<sub>0</sub>

path  
condition



# Concolic Testing Approach



```
int double (int v) {
```

```
    return 2*v;
```

```
}

void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

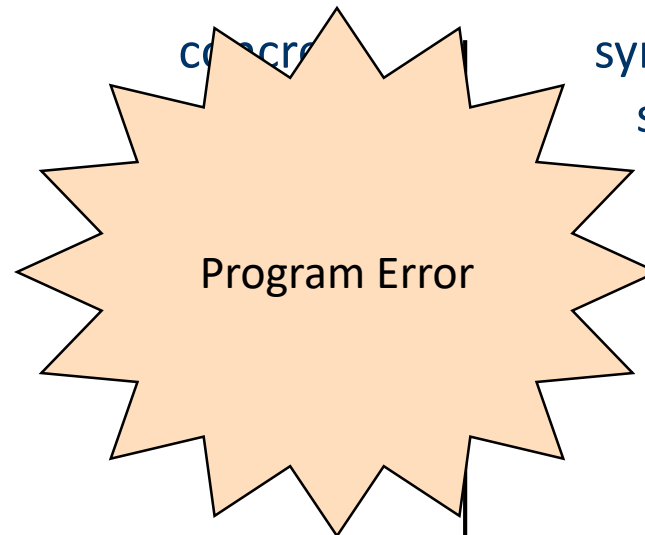
```
        }
```

```
    }
```

```
}
```

Concrete Execution

Symbolic Execution



$x = 30, y = 15$

$x = x_0, y = y_0$



concrete state

symbolic state

path condition

$2 * y_0 == x_0$

$x_0 > y_0 + 10$

# Novelty : Simultaneous Concrete and Symbolic Execution



```
int foo (int v) {
```

```
    return (v*v) % 50;
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete Execution

Symbolic Execution

concrete state

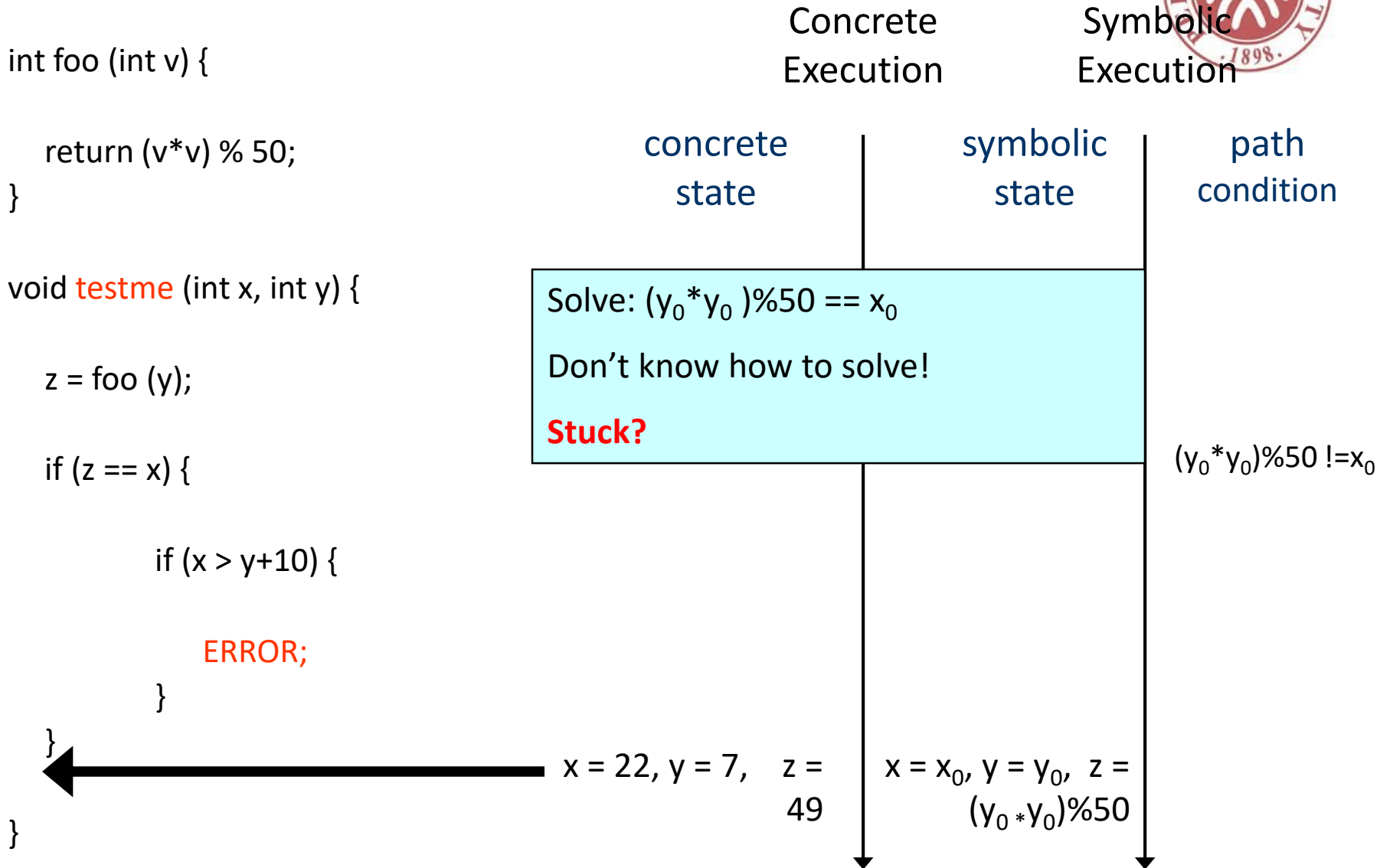
symbolic state

path condition

$x = 22, y = 7$

$x = x_0, y = y_0$

# Novelty : Simultaneous Concrete and Symbolic Execution



# Novelty : Simultaneous Concrete and Symbolic Execution



Concrete Execution

Symbolic Execution

```
void testme (int x, int y) {
    z = foo (y);
    if (z == x) {
        if (x > y+10) {
            ERROR;
        }
    }
}
```

concrete state

symbolic state

path condition

Solve:  $foo(y_0) == x_0$   
 Don't know how to solve!  
**Stuck?**

$foo(y_0) != x_0$

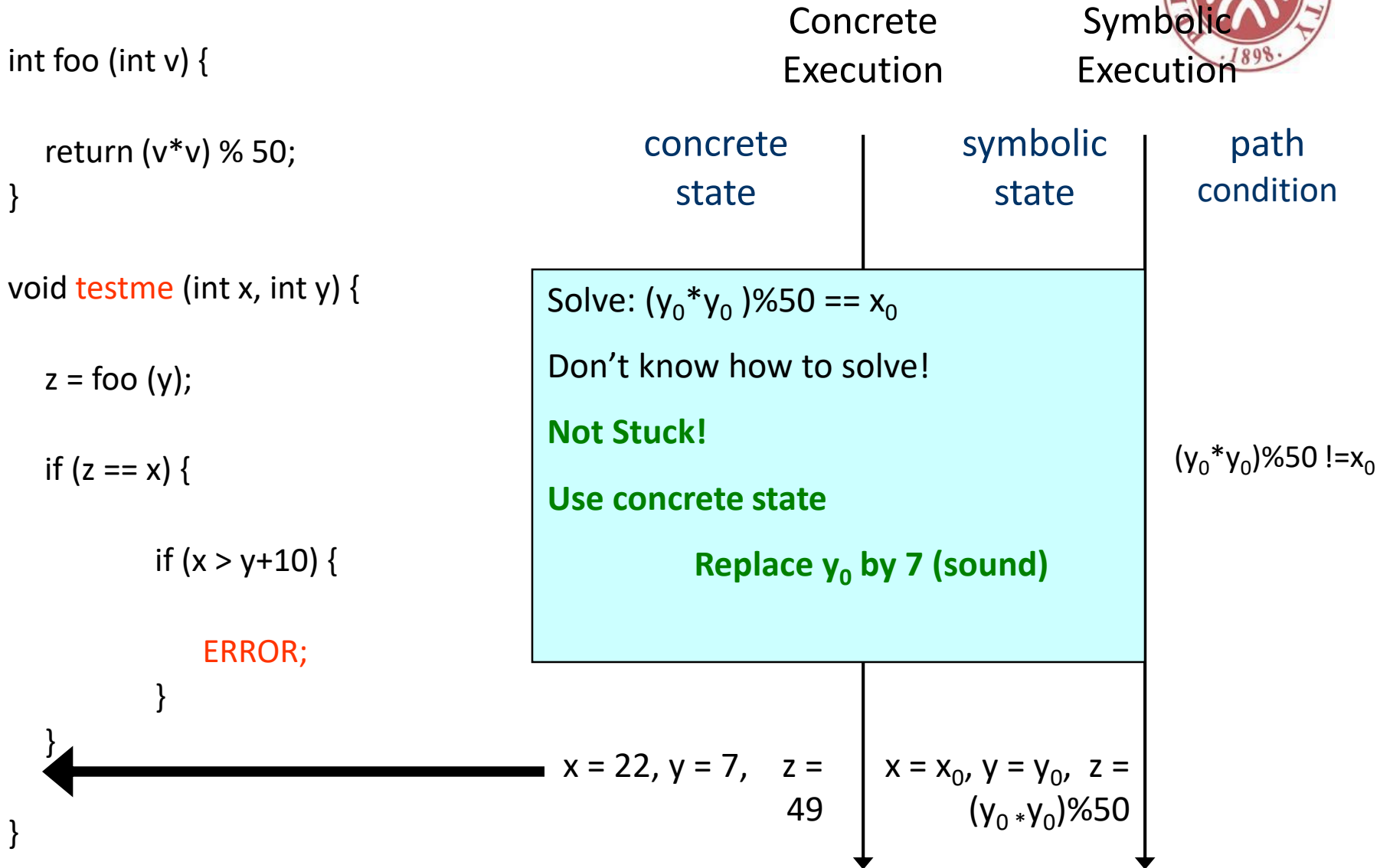
$x = 22, y = 7,$

$z = 49$

$x = x_0, y = y_0, z = foo(y_0)$



# Novelty : Simultaneous Concrete and Symbolic Execution



# Novelty : Simultaneous Concrete and Symbolic Execution



```
int foo (int v) {
```

```
    return (v*v) % 50;
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete Execution

Symbolic Execution

concrete state

symbolic state

path condition

Solve:  $49 == x_0$   
 Solution :  $x_0 = 49, y_0 = 7$

$49 != x_0$

$x = 22, y = 7,$

$z = 48$

$x = x_0, y = y_0,$

$z = 49$



# Novelty : Simultaneous Concrete and Symbolic Execution



```
int foo (int v) {
```

```
    return (v*v) % 50;
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
        }
```

```
    }
```

```
}
```

Concrete Execution

Symbolic Execution

concrete state

symbolic state

path condition

x = 49, y = 7

x = x<sub>0</sub>, y = y<sub>0</sub>



# Novelty : Simultaneous Concrete and Symbolic Execution



```
int foo (int v) {
```

```
    return (v*v) % 50;
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

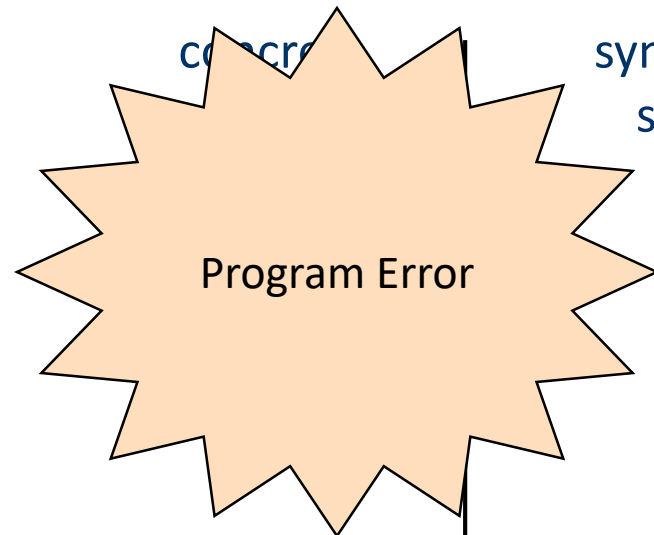
```
        }
```

```
    }
```

```
}
```

Concrete Execution

Symbolic Execution



concrete

symbolic state

path condition

Program Error

$$2 * y_0 == x_0$$

$$x_0 > y_0 + 10$$

$x = 49, y = 7, z = 49$

$x = x_0, y = y_0, z = 49$







# 下周课程

- 由王博同学介绍LLVM
- 方法一
  - 从 <http://pan.baidu.com/s/1c1EujRU> 下载虚拟机，使用 VMWare 12 加载。
  - 密码为 123456。LLVM 根目录为 /home/llvm/llvm/ ， build 目录为/home/llvm/llvm/build/
- 方法二
  - 使用 Linux 或 Mac OS 操作系统（若使用Linux虚拟机推荐内存至少4G）。
  - 按照 <http://llvm.org/docs/GettingStarted.html> 中的 [Getting Started Quickly](#) 提示进行编译。如无调试需要，请在 cmake 时按手册说明使用选项
    - DCMAKE\_BUILD\_TYPE=Release以加快编译速度。